

A recurrent neural model for proto-object based contour integration and figure-ground segregation

Brian Hu¹ • Ernst Niebur^{1,2}

Received: 13 March 2017 / Revised: 22 June 2017 / Accepted: 8 September 2017 / Published online: 19 September 2017 © Springer Science+Business Media, LLC 2017

Abstract Visual processing of objects makes use of both feedforward and feedback streams of information. However, the nature of feedback signals is largely unknown, as is the identity of the neuronal populations in lower visual areas that receive them. Here, we develop a recurrent neural model to address these questions in the context of contour integration and figure-ground segregation. A key feature of our model is the use of *grouping neurons* whose activity represents tentative objects ("proto-objects") based on the integration of local feature information. Grouping neurons, and project modulatory feedback to those same neurons. Additionally, inhibition at both the local feature level and the object representation level biases the interpretation of the visual scene in agreement with principles

Action Editor: B. A. Olshausen

This work is supported by the National Institutes of Health under Grants R01EY027544 and R01DA040990.

Electronic supplementary material The online version of this article (https://doi.org/10.1007/s10827-017-0659-3) contains supplementary material, which is available to authorized users.

☑ Brian Hu bhu6@jhmi.edu

> Ernst Niebur niebur@jhu.edu

¹ Zanvyl Krieger Mind/Brain Institute and Department of Biomedical Engineering, Johns Hopkins University, Baltimore, MD 21218, USA

² Zanvyl Krieger Mind/Brain Institute and Department of Neuroscience, Johns Hopkins University, Baltimore, MD 21218, USA from Gestalt psychology. Our model explains several sets of neurophysiological results (Zhou et al. *Journal of Neuroscience*, 20(17), 6594–6611 2000; Qiu et al. *Nature Neuroscience*, 10(11), 1492–1499 2007; Chen et al. *Neuron*, 82(3), 682–694 2014), and makes testable predictions about the influence of neuronal feedback and attentional selection on neural responses across different visual areas. Our model also provides a framework for understanding how objectbased attention is able to select both objects and the features associated with them.

Keywords Recurrent processing · Shape perception · Feedback · Grouping · Perceptual organization · Contour processing

1 Introduction

Gestalt psychologists recognized the importance of the whole in influencing perception of the parts when they laid out several principles ("Gestalt laws") for perceptual organization (Wertheimer 1923; Koffka 1935). Contour integration, the linking of line segments into contours, and figure-ground segregation, the segmenting of objects from background, are fundamental components of this process. Both require combining local, low-level and global, highlevel information that is represented in different areas of the brain in order to segment the visual scene. The interaction between feedforward and feedback streams carrying this information, as well as the contribution of top-down influences such as attentional selection, are not well understood.

The contour integration process begins in primary visual cortex (V1), where the responses of orientation selective neurons can be modulated by placing collinear stimuli outside the receptive fields (RFs) of these neurons (Stemmler et al.

1995; Polat et al. 1998. Contextual interactions between V1 neurons have often been summarized using a "local association field", where collinear contour elements excite each other and noncollinear elements inhibit each other (Ullman et al. 1992; Field et al. 1993). Results from neuroanatomy lend support to these ideas, as the lateral connections within V1 predominantly link similar-orientation cortical columns (Gilbert and Wiesel 1989; Bosking et al. 1997; Stettler et al. 2002). Computational models based on these types of local interactions have successfully explained the ability of V1 neurons to extract contours from complex backgrounds (Li 1998; Yen and Finkel 1998; Piëch et al. 2013). While some of these models also incorporate feedback connections, the mechanisms by which higher visual areas construct the appropriate feedback signals and target early feature neurons are not clearly specified. One of the main purposes of the present study is to introduce concrete neural circuitry that makes this recurrent structure explicit, thereby allowing us to make quantitative predictions and compare model predictions with experimental data.

Segmenting an image into regions corresponding to objects requires not only finding the contours in the image but also determining which contours belong to which objects. This is part of what is known as the *binding problem*, as it is unclear how higher visual areas "know" which features belong to an object (Treisman 1996). One solution involves differential neural activity, where the neurons responding to the features of an object show increased firing compared with neurons responding to the background. Such response enhancement was first observed in V1 for texture-defined figures (Lamme 1995). Alternatively, it has been proposed that binding is implemented by neurons that represent features of the same object firing in synchrony while neurons representing features of different objects firing asynchronously ("binding by synchrony"; for review see Singer, 1999). While this is an attractive and parsimonious hypothesis, experimental evidence is controversial (Gray et al. 1989; Kreiter and Singer 1992; de Oliveira et al. 1997; Thiele and Stoner 2003; Roelfsema et al. 2004; Dong et al. 2008).

Border-ownership selective cells that have been found in early visual areas, predominantly in secondary visual cortex (V2), appear to be dedicated to this task (Zhou et al. 2000). Border-ownership selective cells encode where an object is located relative to their RFs. When the edge of a figure is presented in its RF, a border-ownership cell will respond with different firing rates depending on where the figure is located. For example, a vertical edge can belong either to an object on the left or on the right of the RF. A border-ownership selective cell will respond differently to these two cases, firing at a higher rate when the figure is located on its "preferred" side, even though the stimulus within its RF may be identical. For a more detailed operational definition of how border-ownership selectivity is determined experimentally, see Section 2.4. Borderownership coding has been studied using a wide variety of artificial stimuli, including those defined by luminance contrast, color contrast, figure outlines (Zhou et al. 2000), motion (von der Heydt et al. 2003), disparity (Zhou et al. 2000; Qiu and von der Heydt 2005), and transparency (Qiu and von der Heydt 2007) as well as, more recently, with faces (Hesse and Tsao 2016) and within complex natural scenes (Williford and von der Heydt 2014, 2016).

To explain this phenomenon, some computational models assume that image context integration is achieved by propagation of neural activity along horizontal connections within early visual areas. Border-ownership information could be generated from the asymmetric organization of surrounds (Nishimura and Sakai 2004, 2005; Sakai et al. 2012) or from a diffusion-like process within the image representation (Grossberg 1994, 1997; Baek and Sajda 2005; Kikuchi and Akashi 2001; Pao et al. 1999; Zhaoping 2005). However, these models have difficulties explaining the fast establishment of border ownership which appears about 25ms after the first stimulus response (Zhou et al. 2000). Propagation along horizontal fibers over the distances used in the experiments would imply a delay of at least \approx 70 ms (Girard et al. 2001, based on the conduction velocity of horizontal fibers in primate V1 cortex; we are not aware of corresponding data for V2). Furthermore, such models are difficult to reconcile with the observation that the time course of border-ownership coding is largely independent of figure size (Sugihara et al. 2011).

An alternative computational model involves populations of grouping (G) cells which explicitly represent (in their firing rates) the perceptual organization of the visual scene (Schütze et al. 2003; Craft et al. 2007). These cells are reciprocally connected to border-ownership selective (B) neurons through feedforward and feedback connections. The combination of grouping cells and the cells signaling local features represents the presence of a "proto-object" (Rensink 2000), resulting in a structured perceptual organization of the scene. Among the operations that can be performed efficiently in the organized scene are tasks that require attention to objects. In our model, attention to an object targets the grouping neurons representing it, rather than, e.g., all low-level features within a visual area that is defined purely spatially (like everything within a certain distance from the center of attention). Therefore attention is directed to proto-objects, resulting in the modulation of B cell activity through feedback from grouping cells (Mihalas et al. 2011). This proto-object based approach is consistent with psychophysical and neurophysiological studies (e.g. Duncan 1984; Egly et al. 1994; Scholl 2001; Kimchi et al. 2007; Qiu et al. 2007; Ho and Yeh 2009; Poort et al. 2012).

Similar to our approach, several other studies also make use of recurrent connections between different visual

areas. Zwickel et al. (2007) studied the influence of feedback projections from higher areas in the dorsal visual stream on border-ownership coding. Feedback in their model is only to the border-ownership selective neurons, so they did not test their model on contour integration tasks. Domijan and Setić (2008) proposed a model involving interactions between the dorsal and ventral visual streams for figure-ground assignment. In their model, there is no explicit computation of border ownership, but instead different surfaces are represented by different firing rates. Jehee et al. (2007) proposed a model of border-ownership coding involving higher visual areas, including areas TE and TEO. In their model, border-ownership assignment depends on the size of the figure, which is directly correlated to the specific level in the visual hierarchy of the model at which an object is grouped. They did not test their model on stimuli with noise, or study the effect of object-based attention. Sajda and Finkel (1995) proposed a complex neural architecture involving contour, surface, and depth modules that performs temporal binding through propagation of neural activity within and between populations of neurons. Tschechne and Neumann (2014) proposed a model quite similar to ours. Their model requires a repeated sequence of filtering, feedback, and center-surround normalization that is solved in an iterative manner. Unlike in our model, V4 neurons in their model do not respond to straight, elongated contours. Also, their model only provides a coarse picture of the timing of contour integration and border-ownership assignment across visual areas. Layton et al. (2012) also proposed a model that performs border-ownership assignment. Their model introduces an additional neuron class ("R cells") that implements competition between grouping cells of different RF sizes (similar to a model by Ardila et al. 2012), and the feedback to B cells is by means of shunting inhibition instead of the gain-modulation that we use in our model.

Previous experimental studies have suggested the involvement of multiple visual areas in contour integration and figure-ground segregation (Poort et al. 2012; Chen et al. 2014). The purpose of the present paper is to extend previous models of perceptual organization (Craft et al. 2007; Mihalas et al. 2011) to explain how feedback grouping circuitry can implement the mechanisms necessary to accomplish both contour integration and figure-ground assignment. Most models mentioned above reproduce results restricted to a single set of experiments (e.g. contour integration or figure-ground segregation). In contrast, our model is able to reproduce results from at least three sets of experiments using the same set of network parameters. Our model provides a general framework for understanding how features can be grouped into proto-objects useful for the perceptual organization of a visual scene. In addition, our model also allows us to explain effects of object-based



Fig. 1 Structure of the model network. Each circle stands for a population of neurons with similar receptive fields and response properties. Magenta, blue, and orange lines represent feedforward excitatory, lateral inhibitory, and feedback excitatory projections, respectively. Edges and other local features of a figure (black dashed parallelogram) activate edge cells (E) whose receptive fields are shown by green ellipses. Edge cells project to border ownership cells (B) that have the same preferred orientation and retinotopic position as the E cells they receive input from. However, for each location and preferred orientation there are two B cell populations with opposite side-of-figure preferences, in the example shown B_L whose neurons respond preferentially when the foreground object is to the left of their receptive fields and B_R whose members prefer the foreground to the right side of their receptive fields. E cells also excite other E cells with the same preferred orientation (connections not shown), as well as a class of inhibitory cells (IE) which, in turn, inhibit E cells of all preferred orientations at a given location. Only E cells of one preferred orientation are shown. B cells have reciprocal, forward excitatory and feedback modulatory connections with two types of grouping cells, G_c and G_o, which integrate global context information about contours and objects, respectively. E cells receive positive (enhancing) modulatory feedback from these same grouping cells. Opposing border ownership cells compete directly via IB cells and indirectly via grouping cells, which bias their activity and thus generate the response differences of opposing border ownership selective neurons. G cell populations also directly excite inhibitory grouping cells (IG; again with the indices L and R), which inhibit G_c cells nonspecifically and G_o cells in all orientations except the preferred one. Top-down attention is modeled as input to the grouping cells and can therefore either be directed towards objects (solid lines) or contours (dashed lines) in the visual field (top)

attention and the role of feedback in parsing visual scenes, areas of research which have not been extensively studied.

2 Materials and methods

2.1 Model structure

The model consists of areas V1, V2, and V4 (Fig. 1). Input comes from a binary-valued orientation map with four orientations $(0, \pi/4, \pi/2, \text{ and } 3\pi/4 \text{ relative to the horizontal})$.

The input signal is first represented in V1 and then propagated to V2 and V4 by feedforward connections. Area V4 provides feedback to lower areas (see Supplementary Material for equations). Neurons in higher areas have larger RFs and represent the image at a coarser resolution. Linear RF sizes in area V4 are four times larger than in V2, which, in turn, are twice as large as those in V1.

To achieve contour integration, we implement mutual excitatory lateral connections between V1 edge (E) cells with the same orientation preference. These connections are similar to the local association fields used in other models (Li 1998; Piëch et al. 2013). Background suppression is carried out through a separate population of inhibitory (IE) cells. The input from V1 edge cells activates border-ownership (B) cells in V2. The B cells inherit their orientation preferences from their presynaptic E cells and for each orientation, there are two B cell populations with opposing side-of-figure preferences. A combination of lateral connections within V2 and feedback connections from V4 (described below) is used to generate border-ownership selectivity. Inhibitory (IB) cells in V2 cause competition between B cells that have the same location and same orientation preference and opposite side-of-figure preference.

In V4, two different types of grouping cells exist. Contour grouping cells (G_c) integrate local edge information and are selective for oriented contours (Fig. 2a). Object grouping cells (G_o) are sensitive to roughly co-circular arrangements of edges, thus implementing Gestalt laws of good continuation, convexity of contour, and compact shape (Fig. 2b). Competition between separate contours and objects is carried out by a population of inhibitory (IG) cells. Grouping (G_c and G_o) cells project back reciprocally to those B cells from which they receive input, and also to the E cells that project to those B cells. This feedback enhances the activity of E cells along contours and biases the competition between B cells to correctly assign border ownership along object boundaries. Importantly, feedback



a

b

connections are modulatory, rather than driving, such that the feedback does not modify activities of cells that do not receive sensory input. Biophysically, this can be achieved if the feedback projections employ glutamatergic synapses of the NMDA type (Wagatsuma et al. 2016).

To model the effect of object-based attention, we assume that areas higher than V4 provide additional excitatory input to those grouping cells whose activity represents the presence of objects or contours in the visual scene, as shown in Fig. 1. This attentional input is driving (as opposed to modulatory) but it is relatively weak; we select its strength as 7% of that of the driving input to the sensory (E) cells. In one part of this study (Section 3.2), we model the effect of a lesion in V4 that removes the feedback completely by setting the weight of feedback connections from V4 to lower areas to zero.

Our approach is an extension of the proto-object-based model of perceptual organization proposed by Mihalas et al. (2011). Different from their approach, we include a new population of contour grouping neurons (the G_c cells) to explain recent results on cortico-cortical interactions during contour integration (Chen et al. 2014). As a result, top-down attention in our model can either be directed to contours or to objects. Our model is also able to reproduce the time course of neural responses in different visual areas, while the Mihalas et al. (2011) model only explains mean neural activities. In order to create more complex input stimuli, we also increased the number of model orientations from two to four. As a simplification to their model, we only include one scale of grouping neurons since we focus on mechanisms that do not require multiple scales.

2.2 Model implementation

Model neuronal populations (usually referred to as "neurons" in the following) are represented by their mean activity (rate coding). The activity is determined by a set of coupled, first-order nonlinear ordinary differential equations which was solved in MATLAB (MathWorks, Natick MA) using standard numerical integration methods. The mean firing rate is necessarily positive, therefore units are simple zero-threshold, linear neurons which receive excitatory and inhibitory current inputs with their dynamics described by,

$$\pi f'(t) = -f + \left[\sum W\right]_+ \tag{1}$$

where f represents the neuron's activity level and τ its time constant, chosen as $\tau = 10^{-2}$ s for all neurons. The sum is over all W which are the neuron's inputs, f' is the first derivative of f with respect to time, and []₊ means halfwave rectification.

All simulations were performed on a 300-core CPU cluster running Rocks 6.2 (Sidewinder), a Linux distribution intended for high-performance computing. A total of 100 simulations were performed for each experimental condition, and our results are based on the mean neural activities averaged over these simulations with different randomly selected stimulus noise patterns, see Sections 2.3 and 2.4.

To constrain our model parameters, we used three sets of neurophysiological data. The first comes from recent contour grouping results (Chen et al. 2014), and our model was able to largely reproduce the magnitude and time course of contour integration at both the V1 and V4 levels. The second comes from studies of border-ownership coding (Zhou et al. 2000) and we show that our model not only explains the emergence of border ownership selectivity but also its approximate time course as reported in that study. The third set of experimental data constraining our model is from the study by Qiu et al. (2007) of the interaction between borderownership selectivity and selective attention. In order to fit the model parameters, we started from the parameters given by Mihalas et al. (2011), and modified them to fit the larger body of experimental results to include contour integration, border-ownership selectivity, and attentional selection.

2.3 Contour integration experiments

For the contour integration experiments reported by Chen et al. (2014), awake behaving monkeys were trained to perform a two-alternative forced-choice task using two simultaneously presented patterns, one containing a contour embedded in noise and one that was noise only (see Fig. 3 for examples). The patterns were composed of 0.25° by 0.05° bars distributed in 0.5° by 0.5° grids. The diameter of the patterns was 4.5°, and the number of bars in the embedded contour was randomly set to 1, 3, 5, or 7 bars within a block of trials in order to control the saliency of the contour. To obtain a reward, the monkey had to saccade to the pattern that contained the contour. When the number of bars was set to 1, both presented stimuli were noise patterns, and the monkey was rewarded randomly with a probability of 50%. While the animals were performing the task, simultaneous single- or multi-unit recordings were made in area V1 and V4 neurons with overlapping receptive fields.

We modeled these experiments by creating visual stimuli contained in a 4.5° by 4.5° area. We "recorded" from the V1 receptive field that was at the center of the stimulus (marked by the yellow circles in Fig. 3), as well as from the corresponding V4 neuron. Input from this area was projected onto a V1 layer of 64×64 neurons, each with a receptive field size of $\sim 0.7^{\circ}$ so the receptive fields overlapped tenfold at each location in the visual field. We divided the input field into a 9×9 grid (each grid point at the center of a 0.5° by 0.5° area) and we placed at each grid location a stimulus bar consisting of three adjacent pixels, corresponding to a size ~ 0.21° by ~ 0.07°. Each stimulus bar had one of four orientations, 0, $\pi/4$, $\pi/2$, or $3\pi/4$. As in the Chen et al. (2014) experiment, contours consisted of 1, 3, 5, or 7 adjacent stimulus bars. We positioned the contour either at the center of the visual field so that the center element of the contour was in the RF of the "recorded" cell (Contour condition, Fig. 3a), or offset from the center of the visual field, such that the "recorded" neuron was *next* to the contour (Background condition, Fig. 3b). We changed the length of the contour by adding bars to both ends of the contour. Due to their size, V4 receptive fields basically enclosed the entire contour. For more details on the stimulus configuration, see Section 3.1.

2.4 Figure-ground segregation experiments

For the figure-ground segregation experiments (Zhou et al. 2000; Qiu et al. 2007; Zhang and von der Heydt 2010), awake, behaving monkeys were trained on a fixation task. Receptive fields of each recorded neuron in areas V1 and V2 were first mapped to determine the optimal stimulus properties for that neuron. Afterwards, in some experiments, a square shape was presented on a uniform gray background with one edge of the square centered on the receptive field of the neuron at the neuron's preferred orientation. In other experiments (results shown in Figs. 9 and S3) the stimulus consisted of two partially overlapping squares, and again the receptive field of the recorded neuron was centered at its preferred orientation on one edge of one of the squares. The size of the square varied between experiments but it was always chosen such that the closest corner was far away from the classical receptive field of the recorded neuron. The square was presented in two positions between which it was "flipped" along the long axis of the neuron's receptive field. For instance, if the preferred orientation was vertical, the square was presented either to the left or the right of the cell's receptive field (we used this example in the choice of the indices in Fig. 1). The difference in the firing rate of the neuron for when the square appears on one side versus the other side is defined as the border-ownership signal. Importantly, in all stimulus conditions, local contents within the receptive field of the neuron remained the same between these two conditions; only global context changed, so the neuron had to integrate information from outside its classical receptive field.

We modeled these experiments by creating visual stimuli that were projected onto the V1 layer. The input to the simulation was either a single square of a size that maximally activated G_o grouping cells of the size chosen in our model, or two partially overlapping squares, as shown in Fig. S3, with each of these squares having the same optimal size. In other models (Craft et al. 2007; Mihalas et al. 2011; Russell et al. 2014), grouping cells of many scales are present, covering the range of possible objects in the input. We calculated border-ownership selectivity at the V2 level using the vector modulation index defined in Section 2.5. In order to create noisy versions of the single square image (Fig. 7), we followed a similar approach as in the contour integration experiments, Section 2.3. We again divided the visual field into a 9×9 grid and we positioned horizontal and vertical bars at specific grid points to generate a square. We then placed a stimulus bar at all other grid points, with their orientations randomly chosen from four possibilities, $0, \pi/4, \pi/2$, and $3\pi/4$.

2.5 Quantitative assessment of border ownership selectivity: vector modulation index

While the border ownership signal discussed in the previous section (the difference in firing rates between presentations of a figure on the two sides of a a neuron's RF) is useful to characterize border-ownership selectivity for that particular neuron, description of population behavior requires a more general measure. We use the vector modulation index, introduced by Craft et al. (2007) and defined by the expression

$$\overrightarrow{\mathbf{v}}(x, y) = m_{\hat{i}}(x, y)\hat{i} + m_{\hat{j}}(x, y)\hat{j}$$
⁽²⁾

where \hat{i} and \hat{j} are unit vectors along the horizontal and vertical image axis, respectively, and the components $m_{\hat{i}}(x, y)$

and $m_{\hat{j}}(x, y)$ are the usual modulation indices along their respective axes, defined as

$$m_{\hat{i}}(x, y) = \frac{\sum_{\theta} B_{\theta}(x, y) \cos \theta}{\sum_{\theta} |B_{\theta}(x, y) \cos \theta|}$$

$$m_{\hat{j}}(x, y) = \frac{\sum_{\theta} B_{\theta}(x, y) \sin \theta}{\sum_{\theta} |B_{\theta}(x, y) \sin \theta|}$$
(3)

Here, $B_{\theta}(x, y)$ is the border ownership signal (difference between the activities of the two opposing B neurons) at the preferred orientation θ at position (x, y), and θ runs over all angles taken into account in the model (four directed orientations in our case, namely $0, \pi/4, \pi/2$, and $3\pi/4$, each with both side-of-figure preferences). Vertical bars in the sums in the denominators indicate absolute values.

Both components in Eq. (3) are limited to values between +1 and -1. For the x-component, for instance, a positive value of $m_i(x, y)$ signifies that the figure is to the right of position (x,y) and a negative value signifies that the figure is to the left. Its absolute value indicates the "strength" of the border-ownership signal, with zero being equivalent to ambivalence between left and right. Corresponding comments apply to the y-component, $m_j(x, y)$, regarding the figure's position upward or downward of (x,y). The direction of the vectorial modulation index $\vec{v}(x, y)$ defined in Eq. (2) indicates the position of the foreground figure in the two-dimensional image plane relative to the point (x,y). For instance, positive values in both components $[m_i(x, y) > 0]$ indicate that the figure is located upwards and to the right of (x,y).



Fig. 3 Normalized V1 *E* cell and V4 G_c cell population responses to contours of varying lengths in either the contour (**a**) or the background (**b**) condition. In (**a**), the "recorded" neuron is on the contour; in (**b**), it is offset from the contour. The top row shows stimuli, the second and third rows show activity in model areas V1 and V4, respectively. Yellow circles mark the RFs of the V1 neurons whose activity is shown in Fig. 4. Activity from model area V2 is not shown because a single contour does not produce clear border ownership selectivity, and the activity in V2 is essentially the same as that in V1, but with reduced spatial resolution due to the

lower number of neurons. Columns in each condition show, from left to right, increasing contour length, with the right-most column showing a jittered stimulus configuration (see text). Neural activity is color coded and normalized to the 7-bar stimulus in both contour and background conditions, with warmer colors representing higher activity (see color bar at right). To avoid unbalanced inputs near the boundaries of the visual field we use periodic boundary conditions. We crop this and all other maps of population activity by one pixel on each side to remove artifacts related to using periodic boundary conditions

3 Results

3.1 Contour enhancement in V1 and V4

We examined contour-related responses in our model using visual stimuli composed of collinear bars among randomly oriented bars (Fig. 3), closely matching the stimuli used in the physiological experiments by Chen et al. (2014). The number of collinear bars constituting an embedded contour was set to either 1, 3, 5, or 7 bars, determining the length of the embedded contour, which also controlled its saliency. When the number of collinear bars was one, the stimulus was identical to a noise pattern. We compared the activity of model neurons whose RFs are centered on the contours or in the noise background (but close to contours) with that obtained in the analogous positions during neurophysiological recordings.

V1 responses were split into those of neurons on contour sites (C-sites) and background sites (B-sites). For contour sites (Fig. 3a), the embedded contour was centered on the

RF of a neuron with a preferred orientation matching that of the contour. For background sites, the contour was laterally placed 0.5° away from the RF center of the recorded neuron, and a background bar was placed in the RF (Fig. 3b), with the contour orientation again matching the preferred orientation of the recorded neuron. Both V1 and V4 neurons along the contour showed increased activity with contour length. Neurons on the background showed increased suppression with contour length. Correspondingly, we show in Fig. 4 the responses of neurons whose preferred orientations align with the contours (yellow circles in Fig. 3).

Except for an input delay of 40 ms corresponding to the duration of visual processing from the retina to V1, we did not add any time delays in the feedforward or feedback connections of our model, as we were not attempting to reproduce any specific latency effects. Nevertheless, our model generally reproduced the dynamics of neural responses to contours in both V1 and V4 observed in the Chen et al. (2014) experiment (Fig. 4a). The most salient feature of the neuronal responses is that the levels of sustained activity



Fig. 4 Normalized V1 *E* cell (contour and background sites) and V4 G_c cell neuronal activity and contour-response d' to contours of varying lengths. **a** V1 contour (top) and background (middle) sites and V4 sites (bottom) showed facilitation followed by saturation with increasing contour length (see legend). V1 background sites showed greater suppression with longer contours. The jitter condition involved a 7-bar pattern where each bar was laterally offset to disrupt collinearity. **b** Corresponding experimental results showing normalized and averaged PSTHs from the Chen et al. (2014) study. **c** Contour-response

d' was higher for the V4 sites compared to the V1 contour sites, and was facilitated by increasing contour length. V1 background sites had increasingly negative d' with longer contours, indicating background suppression. The jitter condition reduced the absolute value of the d'values to close to zero, making it similar to the baseline noise condition. **d** Corresponding experimental observations, showing the mean contour-response d' from the Chen et al. (2014) study. Panels B and D are modified from Figure 2 of Chen et al. (2014). All model results (Panels a and c) are averages for a single neuron over 100 simulations

differ based on the number of bars in the embedded contour. This is observed both for contour sites and for background sites but, importantly, this effect went in opposite directions for these two cases. As the number of collinear bars increased from one to seven, V1 contour sites centered on the contour showed increased activity, with response saturation after five bars. In contrast, V1 background sites that were offset from the embedded contour showed a decrease in activity with increasing number of bars in the background (response suppression). Similar to V1 contour sites, V4 sites showed saturating responses with increasing contour lengths (Fig. 4a, bottom). These results were qualitatively similar to those obtained in the Chen et al. (2014) experiments which are reproduced in Fig. 4b (their Fig. 2a).

The model data also showed strong onset transients in both (contour and background) V1 populations (Fig. 4a, top and center), again in good agreement with experimental results (Fig. 4b, top and center). Transients in V4 neurons were weaker, in both model and experimental data, and nearly absent in the experimental data (though not the model) for longer contours (Fig. 4b, bottom). The transient peak observed in the model results is due to a sharp suppression of the activity level for a short (< 50ms) period which is not observed in the empirical data. We believe that this suppression is due to the strong inhibition at the V4 level between G and IG cells, without equivalent excitation between different G cells.

Following Chen et al. (2014), we quantitatively analyzed the contour responses using the d-prime (d') metric from signal detection theory (Green and Swets 1966), which quantifies the difference in distributions of mean neuronal firing rates between a contour pattern and the noise pattern integrated over the whole interval shown in Fig. 4a, b, i.e. 0-500 ms. Neuronal responses to the 1-bar pattern (the noise pattern) were the baseline for examining contour-related responses in V1 and V4, this pattern therefore had a contourresponse d' of zero. The contour-response d' increased with contour length for both the V1 contour and V4 sites, and d'decreased with contour length for the V1 background sites, Fig. 4c.

The agreement between model (Fig. 4c) and experimental results (Fig. 4d) is striking. One difference we note is that the absolute values of all model d' substantially exceed the corresponding experimental values. This is to be expected since no noise was included in the model (other than the random orientation of input stimulus bars which is also present in the experimental approach) while there are surely multiple sources of noise in the biological system. We have not thoroughly investigated this question but it is highly likely that addition of noise to the model will decrease the d' values.

At first sight, it seems possible that V4 neurons respond with a higher firing rate to longer contours than to shorter ones simply as a consequence of the large size of RFs in V4. In this view, the enhanced responses in V4 with increasing contour length is due to the spatial summation of many bars within the RF at the optimal orientation, independent of their precise location in the RF. To investigate this possiblity, Chen et al. (2014) introduced a "jitter" condition to the 7-bar contour, where alternating collinear bars were laterally offset by a small amount (much less than the receptive field size) in order to disrupt the collinearity of the original contour. They showed that jittering disrupted the contour integration process and reduced the neural responses in V1 and V4 close to baseline levels (Fig. 4b, gray lines). We found the same result in our model, Fig. 4a, gray lines. Furthermore, in the jitter condition, contour-response d'approached baseline for the V1 and V4 sites, as shown in the rightmost points for Fig. 4d for experimental data and Fig. 4c for model results. In both cases, no substantial difference between the jitter condition and the baseline noise condition was observed.

We also investigated the orientation and position dependence of contour-related responses in V1 and V4, and found close agreement of our model results with experimental data (Chen et al. 2014). Due to space constraints, these results are presented in the Supplementary Material. The results for V4 are presented in Supplementary Fig. S1 and the results for V1 are presented in Supplementary Fig. S2.

3.2 The role of feedback and attention in contour grouping

While different forms of attention exist that can be flexibly used for different tasks, we choose here to focus only on the mechanisms of object-based attention (Egly et al. 1994; Scholl 2001; Kimchi et al. 2007; Ho and Yeh 2009). We postulate that attention to objects acts at the level of grouping neurons, in agreement with the Mihalas et al. (2011) model. As shown in that study, modulation of the activity of grouping cells bypasses the need for attentional control circuitry to have access to detailed object features. Instead, grouping neurons are used as "handles" of the associated objects and it is in their interaction with feature-coding neurons that features are assigned to objects. One of the consequences of this mechanism is that the spatial resolution of attentional selection is coarser than visual resolution since the smallest "unit" of spatial attentional deployment is the size of the receptive (and projective) field of grouping cells, which is considerably larger than the receptive fields of featurecoding neurons at the same eccentricity. Behavioral results show strong evidence in favor of this coarse attentional resolution (Intriligator and Cavanagh 2001).

In our model, attention can be directed to objects, including contours. For the contour integration experiments, this is implemented as a top-down input to all contour grouping



Fig. 5 Contour-response d' in V1 E cells (a) and V4 G_c cells (b) for the model with (green) and without attention (black), and for the model with feedback removed (magenta). Attention strongly increased contour-response d' in V4 (b), while the lack of feedback strongly decreased contour-response d' in V1 (a)

neurons at the attended location, but, importantly, there was no direct input to the feature-coding edge (E) cells. As we have seen before (Fig. 4), d' in V1 and V4 populations increases with the number of collinear bars, even in the absence of attention. In addition, we now show that attention increases the contour-response d' for both V1 and V4 neurons, with the additive effect being much larger in V4 than in V1 (Fig. 5). For the 7-bar contours, attention increases the contour-response d' in V1 from 6.08 to 6.66 and in V4 from 7.80 to 11.59. This is consistent with findings that attention has a much larger effect on higher-level neurons compared to early sensory neurons (review: Treue 2001).

One of the advantages of computational modeling is that it allows the study of scenarios that are difficult to implement empirically. One question that is difficult to answer experimentally is how removal of feedback from V4 to lower visual areas would change neuronal responses in V1 and V4, structures that are known to be connected bidirectionally (Zeki 1978; Ungerleider et al. 2007). While it is possible to study the influence of feedback on V2 (and other areas) by cooling (Hupé et al. 1998) or pharmacological inactivation (Jansen-Amorim et al. 2012) of area V4, such manipulations only allow limited control of the effect on multiple brain structures. In contrast, a computational model allows the study of interactions between different areas with perfect control. In the model, we can eliminate all feedback from area V4 simply by "lesioning" the connections from the grouping neurons to the V2 and V1 neurons (setting their strength to zero), thus turning the model into a feedforward network. We found that this has the opposite effect of applying attention on the d' metric: the decrease in contour response d' was much larger in V1 compared to V4. Removing feedback reduced the 7-bar contour-response d'in V1 from 6.08 to 3.77, and in V4 from 7.80 to 6.38 (Fig. 5). We note that the contour-response d' in V1 is above zero even without feedback from grouping neurons because of the contribution of local excitatory connections to contour integration. This asymmetric effect in contour response d' in the two areas (V1 and V4) may point to the different roles of feedforward and feedback processing in early vision. We are not aware of any experimental manipulations that completely remove feedback from area V4 without changing the circuitry in other ways, so our results are a prediction awaiting experimental falsification.

3.3 Border-ownership assignment and highlighting figures in noise

We next apply our model to understanding borderownership assignment, discussed in Section 2.4. We focus first on the standard square figure frequently used in neurophysiological studies of this function (Zhou et al. 2000; Qiu et al. 2007; Sugihara et al. 2011; Williford and von der Heydt 2013, 2014; Martin and von der Heydt 2015). In Fig. 6a, we show the input stimulus, the edge cell activity from area V1 of our model, the border-ownership vector modulation field from V2 (defined in Section 2.5), and the object and contour grouping cell activity from V4. Our model enhances V1 activity along the edges of the square, correctly assigns border ownership in V2 neurons (Zhou et al. 2000, in agreement with), and enhances activity of V4 neurons at the center of the square and the edges of the square (object and contour grouping neurons, respectively).

We also show the time course of the border-ownership signal for a RF located along the left edge of the figure (indicated by the yellow circle in Fig. 6a). The firing rate of a border-ownership selective neuron depends on which side the figure is presented on with respect to its RF. In Fig. 6b, the preferred neuron has a side-of-figure preference to the right (red), while the non-preferred neuron has a sideof-figure preference to the left (blue). The firing rate difference is the border-ownership signal, whose steady-state value is used to compute the vector modulation index \vec{v} (Section 2.5). In Fig. 6c, we show that the border-ownership signal (red) appears rapidly and with short latency compared to the onset of the edge signal (black). Experimental data show that the border-ownership signal appears ~20 ms after the onset of edge responses (Zhou et al. 2000). In our model, the border-ownership signals appears almost instantly. We believe that in addition to visual input, border-ownership cells also receive grouping feedback and that this takes additional time which is not included in our model (see Craft et al. 2007, as an example of a model with latencies).

We then extend this approach by adding additional oriented bars to the stimulus, see Fig. 7. In the top row of the figure, results are shown when the bar orientation within the figure differs from that of the background, similar to the texture-defined figures used in the Lamme (1995) experiments. In the bottom row, bars within and outside the figure



Fig. 6 Figure-ground segregation of a square object as in the Zhou et al. (2000) experiments. **a** Shown left to right are the input stimulus, the edge cell activity (E), the border ownership assignment along edges (shown as the vector modulation index $\vec{\mathbf{v}}$, Section 2.5), the object grouping neuron activity (G_o) and the contour grouping activity (G_c). Activities are normalized within each map, and warmer colors indicate higher activity (see color bar at right). **b** Time course of normalized border-ownership cell activity for the preferred side-of-figure (red) and

are all oriented randomly, similar to the noise stimuli used in the Chen et al. (2014) study. As in Fig. 6, we again show the responses of different populations of neurons in our model. For both types of stimuli, the edges of the square, even when broken up into different bars, are still enhanced while the background bars are suppressed, especially within the square. Interestingly, for the aligned stimulus (top row), only the top and bottom edges of the square show border ownership modulation. This may be an artifact of our modeling procedure, where the edges of our figure are defined by contour elements instead of texture discontinuities. For the noise stimuli (bottom row), border ownership is still assigned correctly along the edge of the square, but the noise results in occasional nonzero border-ownership cell activity at other points in the image as well. For both types of stimuli, grouping cell activity is still centered on the square, and contour grouping neurons still highlight the edges of the squares, but there is also noticeably increased noise.

3.4 Interaction between border ownership assignment and attention

Although border ownership selectivity emerges independently of attention (Qiu et al. 2007), attention may help to facilitate figure-ground segregation in the presence of noise. For the square figure with noise, we found that in our model, attention increases the responses of neurons along the edge of the figure (unpaired t-test, $p = 2.32 \times 10^{-59}$) and

non-preferred side-of-figure (blue) for the receptive field marked by the yellow circle in panel A. Here, the preferred side-of-figure is to the right. **c** Timing of the normalized border-ownership signal (red) and the edge signal (black). The BOS signal is defined as the difference in activities of the two opposing pairs of border-ownership cells in panel B. The edge signal is defined as the sum of the activities of the two border-ownership cells. The curves are normalized to the same scale (0-1) to show the time course of the responses

suppresses those in the center (unpaired t-test, $p = 3.42 \times 10^{-8}$). In addition, attention increases border-ownership modulation along the edge of the figure (unpaired t-test, $p = 1.37 \times 10^{-143}$) and increases the activity of object grouping neurons in the center of the figure (unpaired t-test, $p = 1.53 \times ^{-239}$). All effects were small but highly significant, and were based on the differences in summed activity of neurons along the edge or center of the figure over a total of 100 simulations. Figure 8 shows the average neural activity in the different populations of neurons in our model, with and without the effect of attention.

Attention must also operate in cluttered environments where multiple objects may be present. Qiu et al. (2007) studied border-ownership responses in area V2 when two overlapping squares were presented and attention was directed either to the foreground or background square. Mihalas et al. (2011), using a model closely related to ours but without G_c cells, reproduced the experimental finding that border-ownership modulation was strong when attention was on the foreground figure but weak when attention was on the background figure. Our model reproduces this finding, see Supplementary Fig. S3. The quantitative effect on border-ownership selectivity is shown in Fig. 9. Our model also reproduces the experimental finding that borderownership modulation is strong when attention is on the foreground figure (Fig. 9c, "Front attended") and weak when attention is on the background figure (Fig. 9c, "Back attended").

Fig. 7 Figure-ground segregation of a square object with aligned contour elements (top row) and with noise contour elements (top row). Shown are (left to right) the input stimulus, the edge cell activity (E), the border ownership assignment along edges (shown as the vector

Stimulus

Alignec

Noise

modulation index \vec{v} , Section 2.5), the object grouping neuron activity (G_o) and the contour grouping activity (G_c) . Activities are normalized within each map, and warmer colors indicate higher activity (see color bar at right)

0.4

0.2

0

These results demonstrate that the object and contour grouping neurons are able to assist with early level segmentation of objects in noise and clutter. Previous experimental studies have only tested squares without noise, although the effect of figures defined by broken contours has been investigated before Zhang and von der Heydt (2010). Our results predict that border ownership assignment and grouping are robust even in the presence of noise, clutter, and interruptions in figure borders, and that attention may further aid this process.

4 Discussion

In this study, we use computational models to elucidate the role of attention and feedback in contour and object processing. Different from many models that are tailor-made to reproduce one set of experimental results, we demanded that our model explain data from at least three sets of experimental approaches, (1) contour integration, (2) figure-ground

segregation, (3) attention to objects. We hypothesize that these processes are fundamentally linked in terms of the larger goal of image understanding. Using the same set of model parameters, we reproduced several experimental findings and generated non-trivial predictions.

4.1 Model predictions

Our model predicts that attentional modulation is specific to the attended contour or object, rather than being defined purely spatially. This is possible because, in our model, attention modifies firing rates of grouping cells, rather than of elementary feature-coding cells. Attending to the contour increases contour-response d' in both V1 and V4, consistent with experimental results showing increased contour-related responses after animals had been trained to perform a contour detection task, compared to when they performed a separate set of tasks in which the contour was behaviorally irrelevant (Li et al. 2008). We note that Li et al. (2008) only studied neural responses in V1, while our model makes



Fig. 8 Attentional modulation of different neuronal populations aids figure-ground segregation in the presence of noise. Each panel (a-d) shows the means and standard deviations of neural activity with and without added attention over 100 different simulations. **a** Edge cell activity along the contour of the object shows enhancement with



attention. **b** Edge cell activity in the center of the figure shows suppression with attention. **c** The BOS signal along the contour of the object shows enhancement with attention. **d** Object grouping cell (Go) activity centered on the object shows enhancement with attention



Fig. 9 Quantitative comparison of model performance to neurophysiological findings (Qiu et al. 2007) for border-ownership coding of overlapping figures. **a** The stimulus configurations used are shown, with neurons coding right border ownership (black) and left border ownership (gray) when attention was focused on either foreground square 1 (front attended) or on background square 2 (back attended). **b** The responses of border ownership selective cells recorded in V2

are shown: bars indicate the average firing rate for each stimulus condition. **c** Model B cell responses to analogous stimulus conditions. For both the model and the experiments, border-ownership modulation was strong when attention was on foreground but weak when attention was on background. Panels A and B are modified from Figure 3 of Qiu et al. (2007)

predictions about attention-related changes to contourresponse d' in both V1 and V4. We also find that attention modulates border ownership activity in V2 in an objectbased manner. As a result, our model makes predictions about neural activity in visual areas V1, V2, and V4 across different stimuli and tasks.

We predict that the interaction of modulatory feedback from grouping cells with local inhibition enhances the representation of the figure and suppresses the representation of the background. Indeed, our model produces background suppression for isolated contours as well as for figures embedded in noise. We note that this prediction is different from what others have observed in texture-defined figures (Lamme 1995; Lee et al. 1998), where there is generally response enhancement of the center of the figure. This difference may be due to how the figure is defined, by its contour in our experiment and by texture in Lamme (1995) and Lee et al. (1998). It is possible that if feedback from object grouping neurons is to the center of the figure instead of its edges, we may observe enhancement of activity at the center of the figure. Understanding how border-ownership assignment interacts with filling-in of surfaces is a future direction of research. Furthermore we predict that attention, in addition to enhancing the figure in an object-based manner, also helps to suppress noise in the background.

We also predict that removing feedback from V4 to lower visual areas reduces neural responses in V1, while having a smaller effect in V4. The activity of V4 neurons is also affected due to the recurrency of the network model. This could be tested experimentally by the same contour detection task used by Chen et al. (2014), and measuring the contour-response d' in V1 and V4 from reversible inactivation of feedback connections. Although complete and selective deactivation of V4 feedback to areas V1 and/or

V2 is technically challenging, there have been attempts to study the effect of this type of feedback either through extra-striate lesions (Supèr and Lamme 2007) or reversible inactivation (Jansen-Amorim et al. 2012). Anesthesia presumably also decreases top-down influences, and indeed reduces contour-related V1 responses (Li et al. 2008) and figure-ground segregation (Lamme et al. 1998).

4.2 Comparison to other models

Many have argued that contour integration and figureground segregation are largely local phenomena that rely on lateral connections (Grossberg 1994, 1997; Li 1998; Zhaoping 2005; Piëch et al. 2013). While some of these models include a role for top-down influences (Li 1998; Piëch et al. 2013), they do not offer a specific mechanism by which higher visual areas representing object-level information selectively feed back to lower visual areas containing feature-level information about the object. In contrast, our model is explicit in that feedback connections from higher visual areas modulate the responses of early feature-selective neurons involved in the related processes of contour integration and figure-ground segregation. Our model thus is a member of a broad class of theoretical models that achieve image understanding through bottom-up and top-down recurrent processing (Ullman 1984; Hochstein and Ahissar 2002; Roelfsema 2006; Epshtein et al. 2008). In comparison to similar models, our model is able to reproduce experimental findings from two traditionally separate fields of study- contour integration and figure-ground assignment. Importantly, using the same set of network parameters, the grouping cells in our model are able to represent proto-objects (both contours and extended objects) and provide a perceptual organization of the scene. We show that this perceptual organization is critical for interfacing with top-down attention, and that it provides a general theoretical framework for understanding how feedback connections and an hierarchy of visual areas can be used to group together the features of an object.

4.3 Roles of V1 and V4 in visual processing

While V1 neurons have small RFs that accurately code for orientation, V1 also shows strong background inhibition off the contour. This property allows V1 neurons to enhance contours and suppress noise in the image at a high spatial resolution. V4 neurons, on the other hand, have large RFs that integrate local feature information over large areas of visual space and provide a coarse, proto-object representation of contours and objects. Feedback from V4 can then be refined by the lateral connections present within early visual areas, which aids in the enhancement of the figure and its edges in the image.

Even when V1 neurons receive no feedback from V4, there is an increase in contour-response d' with contour length (Fig. 5). This contour facilitation is solely due to the excitatory lateral connections present in V1, and is weaker without feedback. As a result, feedback from V4 may not be necessary for contour facilitation, but it interacts with local lateral connections in a push-pull manner – neurons along the contour are enhanced, while elements on the back-ground are suppressed. Not surprisingly, removing this type of feedback has a larger effect on V1 neurons compared to V4 neurons, although the activity of V4 neurons is also affected due to the recurrency of the network model.

4.4 Contour and object grouping neurons

Contour grouping neurons have direct experimental support through the recent neurophysiological experiments published by Chen et al. (2014). In our model, relatively few numbers of grouping neurons (both contour and object) are required. The spatial resolution of the grouping process does not need to be very high, as grouping cells only provide a coarse template of the contours and objects present in the scene. Assuming that the activity of grouping cells represents proto-objects with a similar resolution as attention, the total number of grouping cells may be less than 2% of the number of border-ownership cells (Craft et al. 2007). In the contour integration experiments (Chen et al. 2014), many V4 neurons were found to respond to straight, elongated contours, while in our model, only a subset of the grouping neurons are selective for contours. One possible explanation for this is overtraining – monkeys performed the task a very large number of times each day for many months, and neural plasticity may have generated many V4 neurons which respond to contours.

There is no unambiguous neurophysiological evidence for object grouping neurons yet, although previous studies have found neurons in V4 that respond to contour segments of various curvatures (Pasupathy and Connor 2002; Brincat and Connor 2004). The receptive fields of these neurons are similar to those proposed by Craft et al. (2007). Other types of grouping neurons may also exist, including those that respond to gratings (Hegdé and Van Essen 2007), illusory surfaces (Cox et al. 2013), or 3D surfaces (He and Nakayama 1995; Hu et al. 2015). We do not attempt to model the whole array of grouping neurons that may exist, but only those necessary for reproducing the neurophysiological experiments referred to here.

In our model, orientation-independent attentional input to contour grouping cells was used to enhance neural responses to a contour at a given location. We note that this form of attention is analogous to the size- and location tolerant attentional selection process proposed by Mihalas et al. (2011). The local circuitry of their model was able to sharpen a relatively broad and nonspecific attentional input to match the size and location of a figure in the visual scene. Similarly, the local circuitry of our model transforms the orientation-independent attentional input such that it only enhances the contour of the correct orientation. We note that attention also has a suppressive effect in our model, essentially inhibiting unattended objects and locations. There is physiological support for this mechanism (Wegener et al. 2004; Hopf et al. 2006; Sundberg et al. 2009; Tsotsos 2011). Furthermore, previous results show suppression of border-ownership activity along the shared edge of overlapping squares when the back square was attended, but not the front square (Qiu et al. 2007). Finally, psychophysical experiments demonstrate an "object superiority effect," where reaction times are fastest when attention is directed to targets that are part of the cued object, and slowest when targets are outside of an object (Egly et al. 1994; Kimchi et al. 2007).

Complementarily, feature-based attention acts broadly across the visual scene and increases the responses of all components that share similar feature attributes (e.g. color, orientation, or direction of movement) with the attended component (Motter 1994; Treue and Martinez Trujillo 1999). Orientation-specific forms of attention can enhance neural responses in V1 and V4, but do not significantly alter tuning curves or selectivity (McAdams and Maunsell 1999). Our model may be able to reproduce similar results by essentially changing the form of the attentional input to be orientation-specific, i.e. top-down attention targets a *single* population of contour grouping neurons with the same orientation preference. We expect that both object-based and feature-based forms of attention exist and can be flexibly used for different tasks.

4.5 Scope and limitations of the model

Our model seeks to reproduce two different sets of experimental results, while making testable predictions for future experiments. We only included one scale of grouping neurons for simplicity, although multiple scales of grouping neurons are needed to account for the diversity in the scale of objects in the real world. Our model also assigns distinct roles to the different visual areas, edge processing in V1, border ownership assignment in V2, and grouping of contours and objects in V4. However, the physiological properties of neurons in early visual areas have not been fully characterized, and neurons in these different areas may have additional ranges of selectivity than the ones we assign them in our model. Finally, our model operates on artificial images composed of simple shapes such as contours or square figures. In order to truly understand grouping mechanisms in natural vision, our model must also be able to operate on natural images as input, where the number of potential objects and features are much richer. We are currently working on the construction of such a model.

Acknowledgements We would like to thank Justin Killebrew for his help in using the computational cluster in order to run the simulations. We would also like to thank Rüdiger von der Heydt for sharing his deep insights on vision with us.

Compliance with Ethical Standards

Conflict of interests The authors declare that they have no conflict of interest.

References

- Ardila, D., Mihalas, S., von der Heydt, R., & Niebur, E. (2012). Medial axis generation in a model of perceptual organization. In *IEEE CISS-2012 46th Annual conference on information sciences* and systems (pp. 1–4). NJ: IEEE, Princeton University.
- Baek, K., & Sajda, P. (2005). Inferring figure-ground using a recurrent integrate-and-fire neural circuit. *IEEE Transactions on Neural Systems and Rehabilitation Engineering*, 13(2), 125–130.
- Bosking, W.H., Zhang, Y., Schofield, B., & Fitzpatrick, D. (1997). Orientation selectivity and the arrangement of horizontal connections in tree shrew striate cortex. *The Journal of Neuroscience*, 17(6), 2112–2127.
- Brincat, S., & Connor, C. (2004). Underlying principles of visual shape selectivity in posterior inferotemporal cortex. *Nature Neuroscience*, 7, 880–886.
- Chen, M., Yan, Y., Gong, X., Gilbert, C.D., Liang, H., & Li, W. (2014). Incremental integration of global contours through interplay between visual cortical areas. *Neuron*, 82(3), 682–694.
- Cox, M.A., Schmid, M.C., Peters, A.J., Saunders, R.C., Leopold, D.A., & Maier, A. (2013). Receptive field focus of visual area V4 neurons determines responses to illusory surfaces. *Proceedings of the National Academy of Sciences*, 110(42), 17,095–17,100.
- Craft, E., Schütze, H., Niebur, E., & von der Heydt, R. (2007). A neural model of figure-ground organization. *Journal of Neurophysiology*, 97(6), 4310–4326. pMID: 17442769.

- de Oliveira, S.C., Thiele, A., & Hoffmann, K.P. (1997). Synchronization of neuronal activity during stimulus expectation in a direction discrimination task. *Journal of Neuroscience*, 17(23), 9248–9260.
- Domijan, D., & Šetić, M. (2008). A feedback model of figure-ground assignment. *Journal of Vision*, 8(7), 10–10.
- Dong, Y., Mihalas, S., Qiu, F., von der Heydt, R., & Niebur, E. (2008). Synchrony and the binding problem in macaque visual cortex. *Journal of Vision*, 8(7), 1–16. https://doi.org/10.1167/8.7.30. pMC2647779. http://journalofvision.org/8/7/30/.
- Duncan, J. (1984). Selective attention and the organization of visual information. *Journal of Experimental Psychology: General*, 113, 501–517.
- Egly, R., Driver, J., & Rafal, R. (1994). Shifting visual attention between objects and locations: evidence for normal and parietal lesion subjects. *Journal of Experimental Psychology: General*, *123*, 161–177.
- Epshtein, B., Lifshitz, I., & Ullman, S. (2008). Image interpretation by a single bottom-up top-down cycle. *Proceedings of the National Academy of Sciences*, 105(38), 14,298–14,303.
- Field, D.J., Hayes, A., & Hess, R.F. (1993). Contour integration by the human visual system: evidence for a local association field. *Vision Research*, 33(2), 173–193.
- Gilbert, C., & Wiesel, T. (1989). Columnar specificity of intrinsic horizontal and cortico- cortical connections in cat visual cortex. *Journal of Neuroscience*, 9, 2432–2442.
- Girard, P., Hupé, J., & Bullier, J. (2001). Feedforward and feedback connections between areas V1 and V2 of the monkey have similar rapid conduction velocities. *Journal of Neurophysiology*, 85, 1328–1331.
- Gray, C., König, P., Engel, A., & Singer, W. (1989). Oscillatory responses in cat visual cortx exhibit inter-columnar synchronization which reflects global stimulus properties. *Nature*, 338, 334–337.
- Green, D.M., & Swets, J.A. (1966). Signal detection theory and psychophysics. New York: Wiley.
- Grossberg, S. (1994). 3-D vision and figure-ground separation by visual cortex. *Perception & Psychophysics*, 55, 48–120.
- Grossberg, S. (1997). Cortical dynamics of three-dimensional figure– ground perception of two-dimensional pictures. *Psychological Review*, 104(3), 618. pMID 9243966.
- He, Z.J., & Nakayama, K. (1995). Visual attention to surfaces in three-dimensional space. *Proceedings of the National Academy of Sciences USA*, 9(24), 11,155–11,159. pMID 7479956.
- Hegdé, J., & Van Essen, D.C. (2007). A comparative study of shape representation in macaque visual areas V2 and V4. *Cerebral Cortex*, 17(5), 1100–1116.
- Hesse, J.K., & Tsao, D.Y. (2016). Consistency of border-ownership cells across artificial stimuli, natural stimuli, and stimuli with ambiguous contours. *Journal of Neuroscience*, *36*(44), 11,338–11,349.
- Ho, M.C., & Yeh, S.L. (2009). Effects of instantaneous object input and past experience on object-based attention. *Acta Psychologica*, 132(1), 31–39.
- Hochstein, S., & Ahissar, M. (2002). View from the top: hierarchies and reverse hierarchies in the visual system. *Neuron*, 36(5), 791–804.
- Hopf, J., Boehler, C., Luck, S., Tsotsos, J., Heinze, H., & Schoenfeld, M. (2006). Direct neurophysiological evidence for spatial suppression surrounding the focus of attention in vision. *Proceedings of the National Academy of Sciences*, 103(4), 1053. pMID 16410356.
- Hu, B., von der Heydt, R., & Niebur, E. (2015). A neural model for perceptual organization of 3D surfaces. In *IEEE CISS-*2015 49th Annual Conference on Information Sciences and Systems (pp. 1–6). Baltimore: IEEE Information Theory Society. https://doi.org/10.1109/CISS.2015.7086906.

- Hupé, J., James, A., Payne, B., Lomber, S., Girard, P., & Bullier, J. (1998). Cortical feedback improves discrimination between figure and background by V1, V2 and V3 neurons. *Nature*, 394, 784– 787.
- Intriligator, J., & Cavanagh, P. (2001). The spatial resolution of visual attention. *Cognitive Psychology*, 43, 171–216.
- Jansen-Amorim, A.K., Fiorani, M., & Gattass, R. (2012). GABA inactivation of area V4 changes receptive-field properties of V2 neurons in Cebus monkeys. *Experimental Neurology*, 235(2), 553–562.
- Jehee, J.F., Lamme, V.A., & Roelfsema, P.R. (2007). Boundary assignment in a recurrent network architecture. *Vision Research*, 47(9), 1153–1165.
- Kikuchi, M., & Akashi, Y. (2001). A model of border-ownership coding in early vision. In Dorffner, G., Bischof, H., & Hornik, K. (Eds.) *ICANN* (Vol. 2001, pp. 1069–1074).
- Kimchi, R., Yeshurun, Y., & Cohen-Savransky, A. (2007). Automatic, stimulus-driven attentional capture by objecthood. *Psychonomic Bulletin and Review*, 14(1), 166–172.
- Koffka, K. (1935). Principles of Gestalt psychology. New York: Harcourt-Brace.
- Kreiter, A.K., & Singer, W. (1992). Oscillatory neuronal responses in the visual cortex of the awake macaque monkey. *The European Journal of Neuroscience*, 4(4), 369–375.
- Lamme, V.A.F. (1995). The neurophysiology of figure-ground segregation in primary visual cortex. *Journal of Neuroscience*, 15, 1605–1615.
- Lamme, V.A.F., Zipser, K., & Spekreijse, H. (1998). Figure-ground activity in primary visual cortex is suppressed by anesthesia. *Proceedings of the National Academy of Sciences of the United States* of America, 9(6), 3263–3268.
- Layton, O.W., Mingolla, E., & Yazdanbakhsh, A. (2012). Dynamic coding of border-ownership in visual cortex. *Journal of vision*, 12(13), 8.
- Lee, T.S., Mumford, D., Romero, R., & Lamme, V.A.F. (1998). The role of the primary visual cortex in higher level vision. *Vision Research*, 38, 2429–2452.
- Li, Z. (1998). A neural model of contour integration in the primary visual cortex. *Neural Computation*, 10, 903–940.
- Li, W., Piëch, V., & Gilbert, C.D. (2008). Learning to link visual contours. *Neuron*, 57(3), 442–451.
- Martin, A.B., & von der Heydt, R. (2015). Spike synchrony reveals emergence of proto-objects in visual cortex. *The Journal of Neuroscience*, 35(17), 6860–6870.
- McAdams, C.J., & Maunsell, J.H.R. (1999). Effects of attention on orientation-tuning functions of single neurons in macaque cortical area V4. *Journal of Neuroscience*, 19, 431–441.
- Mihalas, S., Dong, Y., von der Heydt, R., & Niebur, E. (2011). Mechanisms of perceptual organization provide auto-zoom and auto-localization for attention to objects. *Proceedings* of the National Academy of Sciences, 108(18), 7583–7588. pMC3088583.
- Motter, B.C. (1994). Neural correlates of attentive selection for color or luminance in extrastriate area V4. *Journal of Neuroscience*, 14, 2178–2189.
- Nishimura, H., & Sakai, K. (2004). Determination of borderownership based on the surround context of contrast. *Neurocomputing*, 58-60, 843–848.
- Nishimura, H., & Sakai, K. (2005). The computational model for border-ownership determination consisting of surrounding suppression and facilitation in early vision. *Neurocomputing*, 65, 77–83.
- Pao, H.K., Geiger, D., & Rubin, N. (1999). Measuring convexity for figure/ground separation. In 7th international conference on computer vision. Kerkyra.

- Pasupathy, A., & Connor, C.E. (2002). Population coding of shape in area V4. *Nature Neuroscience*, 5(12), 1332–1338.
- Piëch, V., Li, W., Reeke, G.N., & Gilbert, C.D. (2013). Network model of top-down influences on local gain and contextual interactions in visual cortex. *Proceedings of the National Academy of Sciences*, *110*(43), E4108–E4117. pMC3808648.
- Polat, U., Mizobe, K., Pettet, M.W., Kasamatsu, T., & Norcia, A.M. (1998). Collinear stimuli regulate visual responses depending on cell's contrast threshold. *Nature*, 391, 580–584.
- Poort, J., Raudies, F., Wannig, A., Lamme, V.A., Neumann, H., & Roelfsema, P.R. (2012). The role of attention in figure-ground segregation in areas V1 and V4 of the visual cortex. *Neuron*, 75(1), 143–156.
- Qiu, F.T., & von der Heydt, R. (2005). Figure and ground in the visual cortex: V2 combines stereoscopic cues with Gestalt rules. *Neuron*, 47, 155–166.
- Qiu, F.T., & von der Heydt, R. (2007). Neural representation of transparent overlay. *Nature Neuroscience*, 10(3), 283–284.
- Qiu, F.T., Sugihara, T., & von der Heydt, R. (2007). Figure-ground mechanisms provide structure for selective attention. *Nature Neuroscience*, 10(11), 1492–1499.
- Rensink, R.A. (2000). The dynamic representation of scenes. Visual Cognition, 7(1/2/3), 17–42.
- Roelfsema, P.R. (2006). Cortical algorithms for perceptual grouping. Annual Review of Neuroscience, 29, 203–227.
- Roelfsema, P.R., Lamme, V.A.F., & Spekreijse, H. (2004). Synchrony and covariation of firing rates in the primary visual cortex during contour grouping. *Nature Neuroscience*, 7(9), 982–991. https://doi.org/10.1038/nn1304.
- Russell, A.F., Mihalas, S., von der Heydt, R., Niebur, E., & Etienne-Cummings, R. (2014). A model of proto-object based saliency. *Vision Research*, 94, 1–15.
- Sajda, P., & Finkel, L. (1995). Intermediate-level visual representations and the construction of surface perception. *Journal of Cognitive Neuroscience*, 7, 267–291.
- Sakai, K., Nishimura, H., Shimizu, R., & Kondo, K. (2012). Consistent and robust determination of border ownership based on asymmetric surrounding contrast. *Neural Networks*, 33, 257– 274.
- Scholl, B.J. (2001). Objects and attention: the state of the art. Cognition, 80(1-2), 1–46.
- Schütze, H., Niebur, E., & von der Heydt, R. (2003). Modeling cortical mechanisms of border ownership coding. *Journals of Vision*, 3(9), 114a.
- Singer, W. (1999). Neuronal synchrony: a versatile code for the definition of relations? *Neuron*, 24, 49–65.
- Stemmler, M., Usher, M., & Niebur, E. (1995). Lateral cortical connections may contribute to both contour completion and redundancy reduction in visual processing. *Society for Neuroscience Abstracts*, 21(1), 510.
- Stettler, D.D., Das, A., Bennett, J., & Gilbert, C.D. (2002). Lateral connectivity and contextual interactions in macaque primary visual cortex. *Neuron*, 36(4), 739–750.
- Sugihara, T., Qiu, F.T., & von der Heydt, R. (2011). The speed of context integration in the visual cortex. *Journal of Neurophysiology*, 106(1), 374–385. pMC3129740.
- Sundberg, K.A., Mitchell, J.F., & Reynolds, J.H. (2009). Spatial attention modulates center-surround interactions in macaque visual area v4. *Neuron*, 61, 952–963.
- Supèr, H., & Lamme, V.A. (2007). Altered figure-ground perception in monkeys with an extra-striate lesion. *Neuropsychologia*, 45(14), 3329–3334.
- Thiele, A., & Stoner, G. (2003). Neuronal synchrony does not correlate with motion coherence in cortical area MT. *Nature*, 421(6921), 366–370.

- Treisman, A. (1996). The binding problem. Current Opinion in Neurobiology, 6(2), 171–178.
- Treue, S., & Martinez Trujillo, J.C. (1999). Feature-based attention influences motion processing gain in macaque visual cortex. *Nature*, 399, 575–579.
- Treue, S. (2001). Neural correlates of attention in primate visual cortex. *Trends in Neurosciences*, *24*, 295–300.
- Tschechne, S., & Neumann, H. (2014). Hierarchical representation of shapes in visual cortex—from localized features to figural shape segregation. *Frontiers in computational neuroscience*, 8, 93.
- Tsotsos, J.K. (2011). A computational perspective on visual attention. MIT Press.
- Ullman, S. (1984). Visual routines. Cognition, 18, 97-159.
- Ullman, S., Gregory, R., & Atkinson, J. (1992). Low-level aspects of segmentation and recognition [and discussion]. *Philosophical Transactions of the Royal Society of London Series B: Biological Sciences*, 337(1281), 371–379.
- Ungerleider, L.G., Galkin, T.W., Desimone, R., & Gattass, R. (2007). Cortical connections of area V4 in the macaque. *Cerebral Cortex*, 18(3), 477–499.
- von der Heydt, R., Qiu, F.T., & He, Z.J. (2003). Neural mechanisms in border ownership assignment: motion parallax and gestalt cues. *Journal of Vision*, 3(9), 666a.
- Wagatsuma, N., von der Heydt, R., & Niebur, E. (2016). Spike synchrony generated by modulatory common input through NMDAtype synapses. *Journal of Neurophysiology*, 116(3), 1418–1433.
- Wegener, D., Freiwald, W.A., & Kreiter, A.K. (2004). The influence of sustained selective attention on stimulus selectivity in macaque visual area mt. *Journal of Neuroscience*, 24(27), 6106–6114.

- Wertheimer, M. (1923). Untersuchungen zur Lehre von der Gestalt II. Psychologische Forschung, 4, 301–350.
- Williford, J.R., & von der Heydt, R. (2013). Border-ownership coding. Scholarpedia, 8(10), 30,040.
- Williford, J.R., & von der Heydt, R. (2014). Early visual cortex assigns border ownership in natural scenes according to image context. *Journal of Vision*, 14(10), 588–588.
- Williford, J.R., & von der Heydt, R. (2016). Figure-ground organization in visual cortex for natural scenes. *eNeuro*, 3(6), ENEURO– 0127.
- Yen, S.C., & Finkel, L.H. (1998). Extraction of perceptually salient contours by striate cortical networks. *Vision Research*, 38(5), 719– 741.
- Zeki, S.M. (1978). Uniformity and diversity of structure and function in rhesus monkey prestriate visual cortex. *The Journal of Physiology*, 277(1), 273–290.
- Zhang, N., & von der Heydt, R. (2010). Analysis of the context integration mechanisms underlying figure–ground organization in the visual cortex. *The Journal of Neuroscience*, 30(19), 6482–6496. pMC2910339.
- Zhaoping, L. (2005). Border ownership from intracortical interactions in visual area V2. *Neuron*, 47, 43–153. pMID 15996554.
- Zhou, H., Friedman, H.S., & von der Heydt, R. (2000). Coding of border ownership in monkey visual cortex. *Journal of Neuroscience*, 20(17), 6594–6611. pMID 10964965.
- Zwickel, T., Wachtler, T., & Eckhorn, R. (2007). Coding the presence of visual objects in a recurrent neural network of visual cortex. *Bio Systems*, 89(1), 216–226.